

Register Number:

DATE: 02-12-2020 *

ST. JOSEPH'S COLLEGE (AUTONOMOUS), BENGALURU-27

B.Sc. STATISTICS - V SEMESTER

SEMESTER EXAMINATION - NOVEMBER 2020

ST 5118: SAMPLING THEORY AND DESIGNS OF EXPERIMENTS

Time: 2 1/2 Hours

Max: 70 Marks

This question paper has TWO printed pages and THREE parts.

PART - A

I Answer any FIVE of the following:

5 x 3= 15

- 1. Define pilot survey
- 2. Give any three methods to control non sampling error
- 3. Explain the concept of equal probability sampling
- 4. List out the principles of Design of Experiments. Explain any one of them
- 5. Define contrast. Give an example
- 6. Write a short note on Tuckey's test
- 7. For a simple random sample of size 100, the 95% confidence interval for population mean is (48.04, 51.96). Estimate population standard deviation using information provided. (Critical value = 1.645)

PART - B

II Answer any FIVE of the following:

 $5 \times 7 = 35$

- 8. A) Write a short note on determination of sample size under simple random sampling without replacement
 - B)In systematic sampling, prove that sample mean is an unbiased estimator of population mean (4+3)
- 9. A)Show that sample variance s² is an unbiased estimator of population variance S² under simple random sampling without replacement.
 - B)Briefly explain proportional allocation in stratified random sampling (5+2)
- 10. A)Compare stratified random sampling and cluster sampling
 - B)Definecluster sampling mean and show that it is unbiased for population mean when the clusters are of equalsize (3+4)

- 11. Derive the least square estimator of parameters for Completely Randomized Design (7)
- 12. A) Explain the construction of Yates table for 2³ factorial experiments

B) In 2² design show that main effects are orthogonal contrast.

(5+2)

13. A) State the assumptions of one-way analysis of variance.

B) Find (a), (b), (c), (d),(e) in the following ANOVA table and state your conclusion (3+4)

Source of variation	Degrees of freedom	Sum of squares	Mean squares	F ratio	F critical
Due to Treatments	4	16.58	(d)	(e)	3.48
Due to Errors	(a)	(c)	0.455		
Total	(b)	21.13			

14. Give the mathematical model of randomized block design when m observations per cell and the explain the method of computing treatment sum of squares (7)

PART - C

III Answer any TWO of the following:

 $2 \times 10 = 20$

- 15. A) Mention any four methods of primary data collection. Explain any one of them.
 - B)Derive the variance of sample mean under SRSWR

(5+5)

- 16. A)What is stratification? State its need. If SRSWOR used within each stratum derive the formula for variance of stratified sample mean.
 - B) Explain linear systematic sampling

(6+4)

- 17. A) What is complete confounding? In a 2³ experiment, write the layout for a replicate with the effect ABC confounded.
 - B) Explain the analysis of Latin square design

(4+6)