

ST. JOSEPH'S COLLEGE (AUTONOMOUS), BANGALORE-27
MID SEMESTER TEST- AUGUST 2016
M.Sc. MATHEMATICS- III SEMESTER
MT DE 9416 : MATHEMATICAL METHODS

TIME: 1 HOUR

MAX. MARKS: 20

Answer any FOUR questions.(5 marks)

$$5 \times 4 = 20$$

1. Solve the Fredholm integral equation $\Psi(x) = x + 2 \int_0^1 (xy^2 + x^2 y) \Psi(y) dy$
2. Solve the Volterra integral equation $\Psi(x) = \sqrt{x} + \lambda \int_0^x \sqrt{xy} \Psi(y) dy$
3. Derive the expression for Neumann series for kernel of Fredholm integral equations.
4. Derive the expression for the resolvent kernel of Volterra integral equation.
5. $y'' - 5y' + 6y = 0, y(0) = 0, y'(0) = -1$ Obtain the integral equation corresponding to the differential equation.
6. Find the eigen values of the integral equation $\Psi(s) = g(s) + \lambda \int_0^1 (s+t) \Psi(t) dt$