

Register Number: DATE:

ST. JOSEPH'S COLLEGE (AUTONOMOUS), BANGALORE-27

M.Sc. PHYSICS - I SEMESTER

SEMESTER EXAMINATION- OCTOBER 2018

PH 7518 - ANALYTICAL TOOLS FOR MATHEMATICAL PHYSICS

Time-1 hr. Maximum Marks-30

This question paper has 2 printed pages and 1 part

Answer any THREE full questions.

(3x10=30)

1. Consider the vectors
$$|u\rangle = \begin{pmatrix} 1\\3+2i\\8i \end{pmatrix}$$
 and $|v\rangle = \begin{pmatrix} 4+3i\\\sqrt{3}i\\1 \end{pmatrix}$.

- (a) Calculate $||u\rangle||$ and $||v\rangle||$ (2 marks)
- (b) Compute $\langle u|v\rangle$ (1 mark)
- (c) Normalize each of the vectors (2 marks)
- (d) Find the angle between the two vectors (2 marks)
- (e) Compute the outer product $|v\rangle\langle u|$ (3 marks)
- 2. Consider a mathematician who uses the vectors $|e_1\rangle=\begin{pmatrix}1\\-1\end{pmatrix}$, $|e_2\rangle=\begin{pmatrix}-2\\0\end{pmatrix}$ as his basis vectors.
 - (a) If he wants to transform into the cartesian space, what should his transformation matrix be? (3 marks)
 - (b) If the matrix $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$ is the rotation matrix for a rotation of angle $\theta = 90^{\circ}$, what is the equivalent matrix in the mathematician's space? (7 marks)

3. Consider the vectors:
$$|a\rangle = \begin{pmatrix} 1\\0\\3 \end{pmatrix}$$
, $|b\rangle = \begin{pmatrix} 1\\-1\\3 \end{pmatrix}$ and $|c\rangle = \begin{pmatrix} 2\\-1\\-1 \end{pmatrix}$.

(a) Perform Gram-Schmidt orthogonalization

(6 marks)

(b) Normalize the vectors

(4 marks)

- 4. Consider the system of linear equations 0.28 x + 9.24 y = 38.641.44 x + 0.1 y = 4.62
 - (a) Can this equation be solved? If yes, find the solution using Gauss elimination and if not elucidate. (3 marks)
 - (b) Consider the coefficient matrix for the same system
 - i. Find the eigen values for the matrix

(3 marks)

ii. Find the corresponding eigen vectors

(4 marks)