



Date:

Registration number:

**ST. JOSEPH'S UNIVERSITY, BENGALURU -27**  
**BCA (DATA ANALYTICS) – II SEMESTER**  
**SEMESTER EXAMINATION: APRIL 2024**  
(Examination conducted in MAY/JUNE 2024)  
**BCADA 2321: Discrete Mathematics II**  
(For current batch students only)

**Time: 2 Hours**

**Max Marks: 60**

**This paper contains TWO printed pages and THREE parts**

**PART A**

**ANSWER ALL THE QUESTIONS**

**5 X 2 = 10**

1. Find the rank of the matrix  $\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & 3 & 4 \\ 1 & 3 & 5 & 7 \\ 1 & 4 & 7 & 10 \end{bmatrix}$  using Row reduced echelon form.
2. When do we say a set of vectors is linearly dependent?
3. Find the solution of  $\int 5x(x^2+3)dx$
4. Why do we need to use Integration?
5. Mention any two states of finite automata machine.

**PART B**

**ANSWER ANY FIVE QUESTIONS**

**5 X 4 = 20**

6. Find the non-trivial solution of the given simultaneous equations.  
 $x + y = 0$   
 $x - y = 0$   
 $3x + y - z = 0$
7. Examine the consistency of the following system of equations  
 $x + 2y - z = 3$   
 $3x - y + 2z = 1$   
 $2x - 2y + 3z = 2$
8. Show that the vector  $(2,2,3)$  is in the span of the vectors  $(2,1,4)$ ,  $(1,-1,3)$ ,  $(3,2,5)$
9. Find the linear transformation  $f: \mathbb{R}^2 \rightarrow \mathbb{R}^2$  such that  $f(1,0) = (1,1)$  and  $f(0,1) = (-1,2)$
10. Find the value of  $\int (5x^4 + 3x^3 - 5x - 2e^x) dx$
11. Find the value of  $\int 2x \sin x dx$
12. Describe finite state machine.

**PART C**

**ANSWER ANY THREE QUESTIONS**

**3 X 10 = 30**

13. Find the eigen values and corresponding eigen vectors of the matrix  $A = \begin{bmatrix} 1 & 2 \\ 3 & 2 \end{bmatrix}$
14. Find the dimension and basis of the subspace of  $V$  spanned by subset  $S$  given by  $S = \{(2,4,2), (1,-1,0), (1,2,1) \text{ and } (0,3,1)\}$
15. Find the value of  $\int e^x \sin x \, dx$
16. Draw with a neat state diagram of the simplified Ticketing machine.